

# Origine and transport of radon in wet and dry mofettes of Covasna Town, Romania

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# MAGYARORSZÁG

## HEGYRAJZI ES VIZRAJZI TÉRKÉPE

A vallás és közoktatásügyi (nádor) miniszter engedélyével

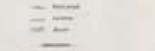
**KOGUTOWICZ MŰMŐ.**

KIADJAA MAGYAR FÖLDRAJZI INTÉZET RT. BUDAPESTEN.

MÉRTÉK 1:400000

AMÉRTŐSÉGI TITOKZATÁSOK

### JEL ÉS SZÍNVAGYRÁZAT.

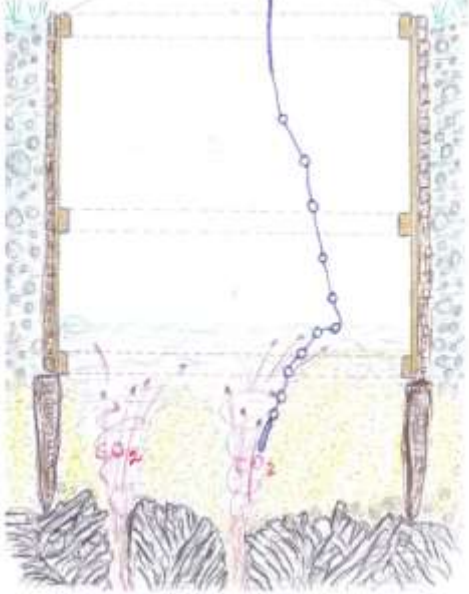


### RÖVIDÍTÉSEK.

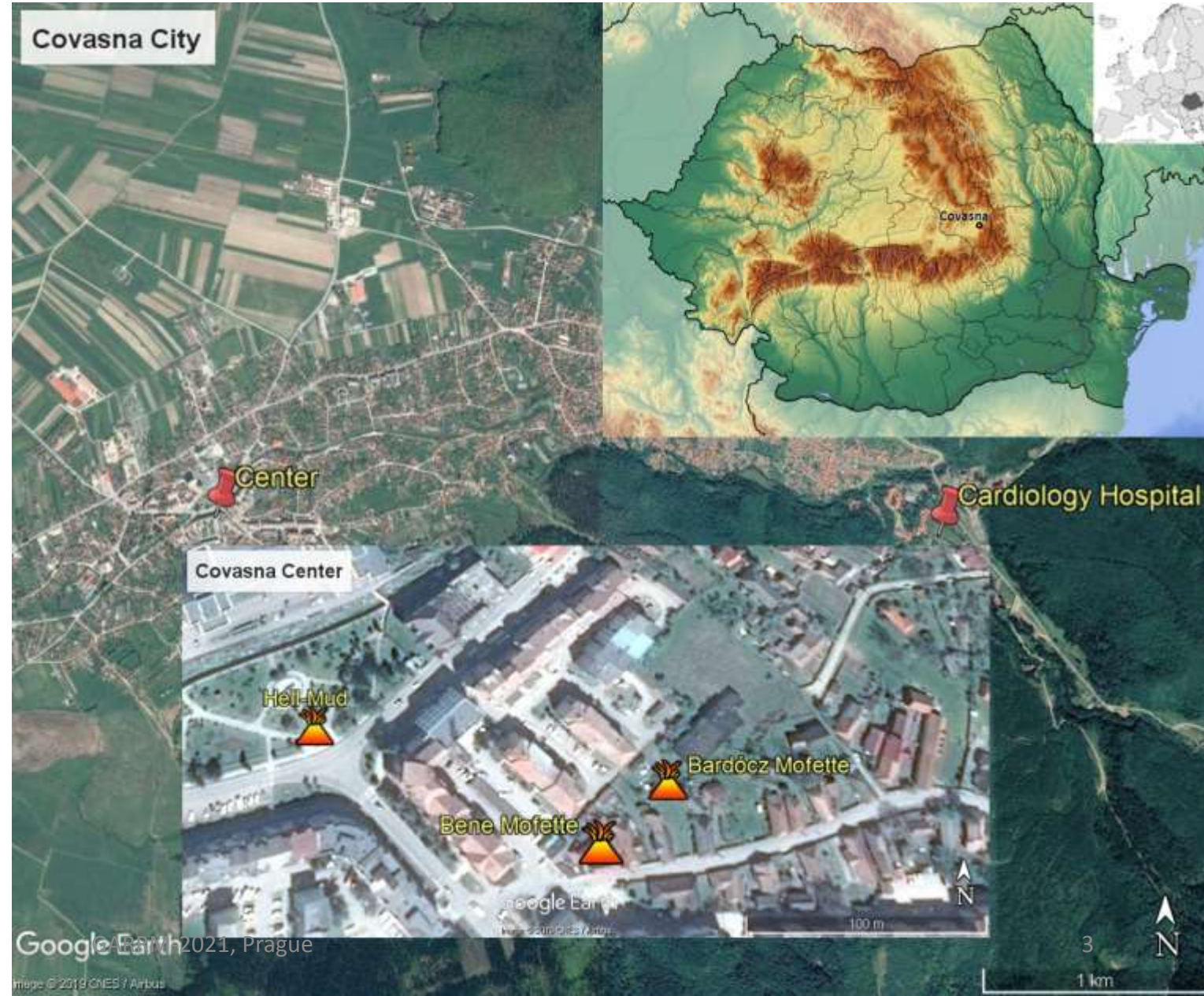
- |                     |                      |
|---------------------|----------------------|
| 1. Székelyföld      | 11. Szigetköz        |
| 2. Erdély           | 12. Győr-Ménfőcsanak |
| 3. Kárpát-medence   | 13. Bükk             |
| 4. Kisalföld        | 14. Mátyásföld       |
| 5. Alföld           | 15. Hortobágy        |
| 6. Délkelet-alföld  | 16. Balaton-felvidék |
| 7. Délkelet-alföld  | 17. Mátyásföld       |
| 8. Délkelet-alföld  | 18. Mátyásföld       |
| 9. Délkelet-alföld  | 19. Mátyásföld       |
| 10. Délkelet-alföld | 20. Mátyásföld       |

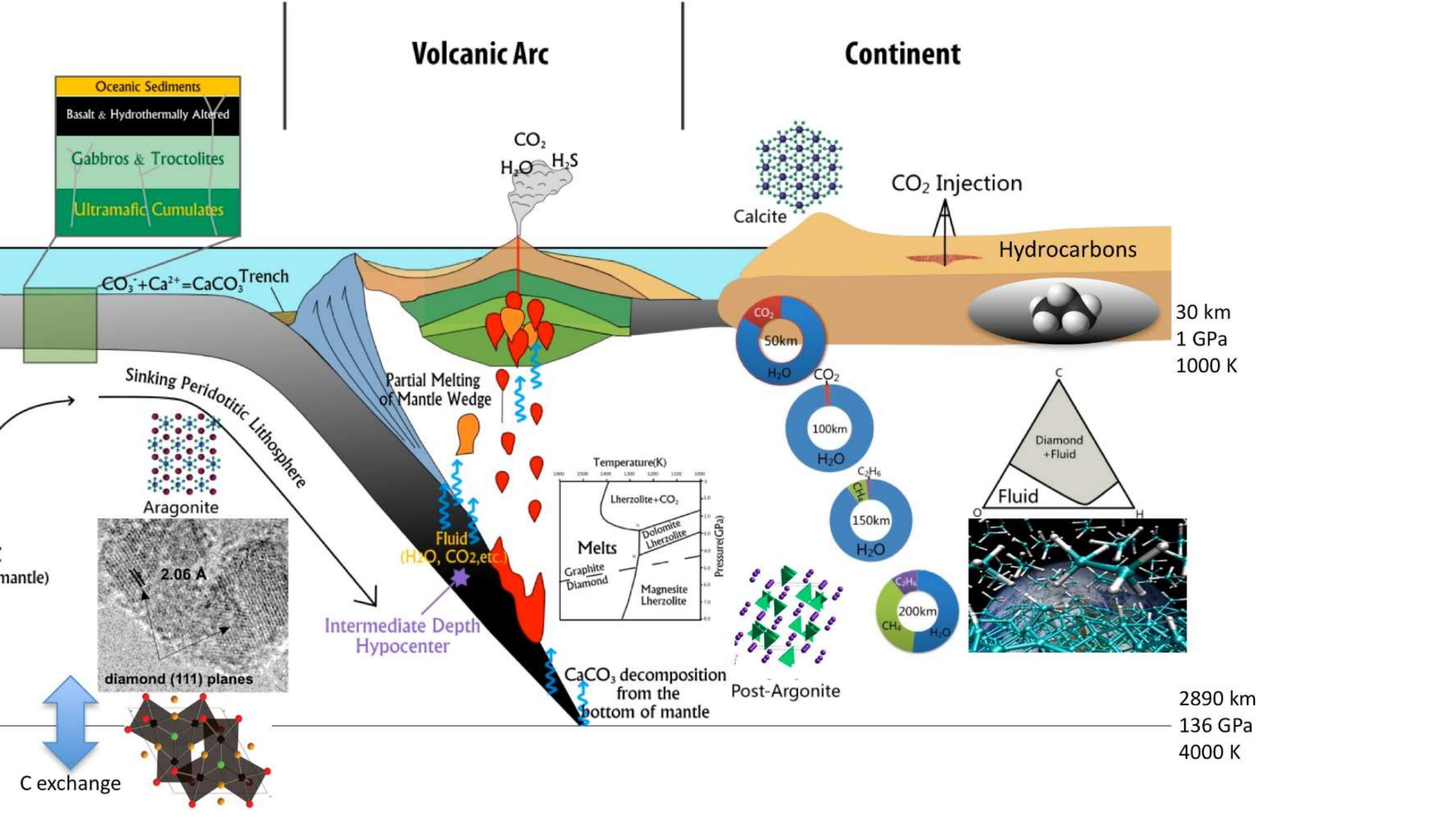


# Pokolsár, wet mofette of Covasna, Romania



2021. 09. 20-23.

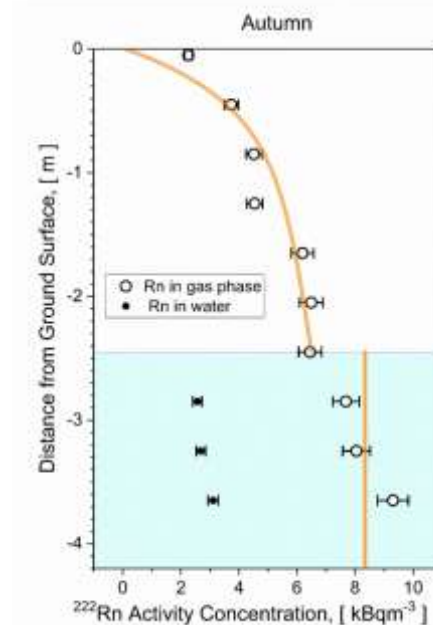
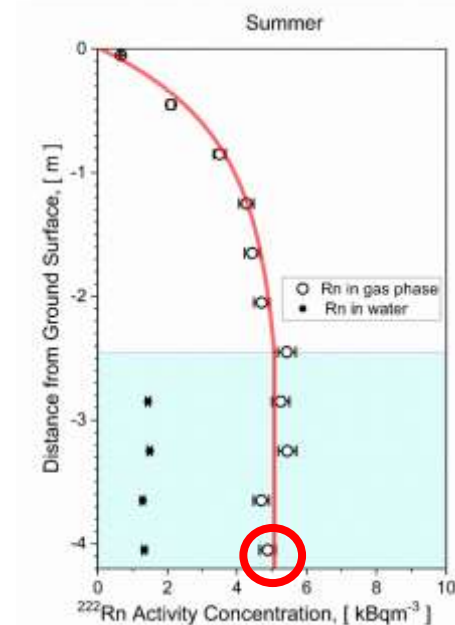
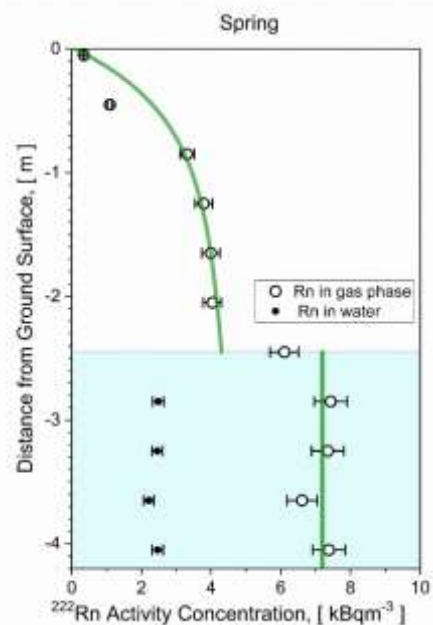
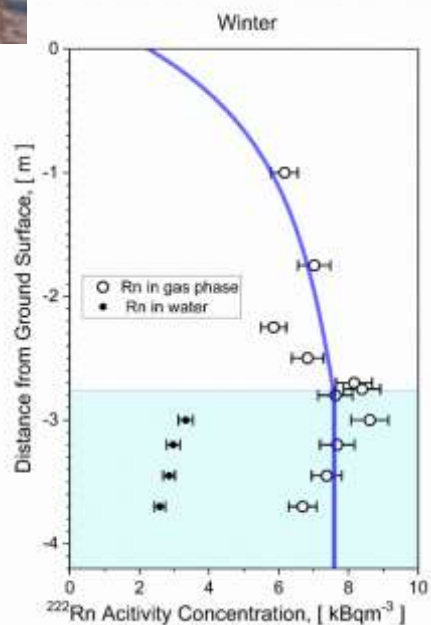
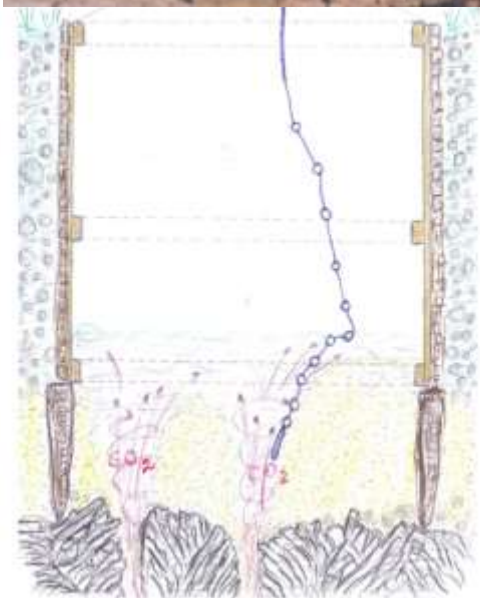




# Pokolsár, wet mofette of Covasna, Romania



Results of measurements and model calculations



# Pokolsár, wet mofette of Covasna, Romania



## Model

Spatial variation of  $^{222}\text{Rn}$  activity concentration in deep bedrock and sedimentary rocks:

$$D_i \frac{d^2 C}{dz^2} - v \frac{dC}{dz} + G_i - \lambda C = 0$$

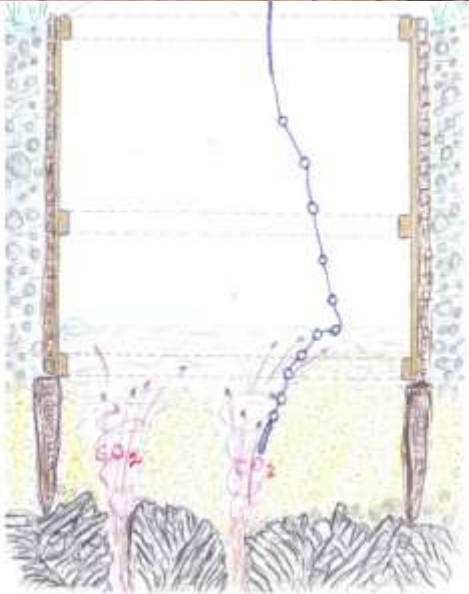
where

$C(z)$  is the  $^{222}\text{Rn}$  activity concentration in the liquid phase that completely fills the pore space ( $\text{Bq m}^{-3}$ ),

$D_i$  is dispersion coefficient,

$G_i$  is Rn-source term,

$v$  is the average interstitial velocity of groundwater.



# Pokolsár, wet mofette of Covasna, Romania



## Model

The radon balance equation for the water in the pool of the Hell-mud (Pokolsár) is:

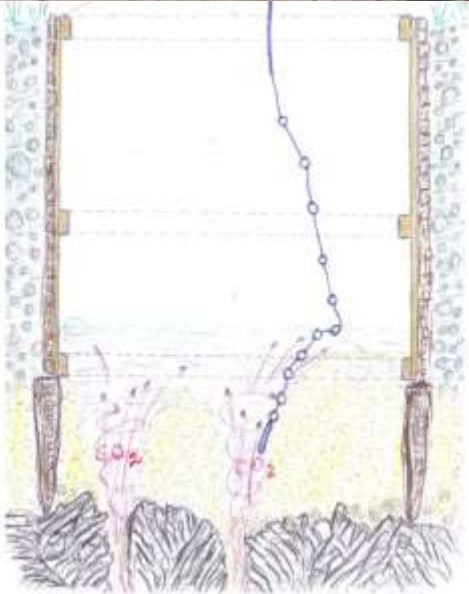
$$\frac{dC_w}{dt} = \frac{1}{z_2 - z_1} (j_2(z_2) - j_b - v\phi C_w) - \lambda C_w .$$

Here  $j_2(z_2)$  is the bulk  $^{222}\text{Rn}$  activity flux density at the bottom of the pool, which can be specified as:

$$j_2(z_2) = (v - D\gamma_2)e^{\gamma_2 z_2} \phi C_{s0} + v\phi \frac{G_s}{\lambda} .$$

$j_b$  is the  $^{222}\text{Rn}$  activity flux density transported from the water to the gas phase of the pool by bubbles. This term is obtained by multiplying the volume flux density  $Q_{bV}$  of carbon dioxide gas in the bubbles ( $\text{m}^3/\text{m}^2\text{s}$ ) and the  $^{222}\text{Rn}$  activity concentration in bubbles ( $C_b = C_w/H^{cc}$ ).

$$j_b = Q_{bV} C_b .$$



# Pokolsár, wet mofette of Covasna, Romania



## Model

The  $^{222}\text{Rn}$  activity concentration in bubbles is related to the  $^{222}\text{Rn}$  activity concentration in the water ( $C_w$ ) through the Henry's partition coefficient ( $H^{cc}$ ), the temperature dependence of which is given as

$$H^{cc}(T) = \frac{C_w}{C_b} = H^{cp}(T) R T = H_0^{cp} R T e^{\alpha\left(\frac{1}{T} - \frac{1}{T_0}\right)}$$

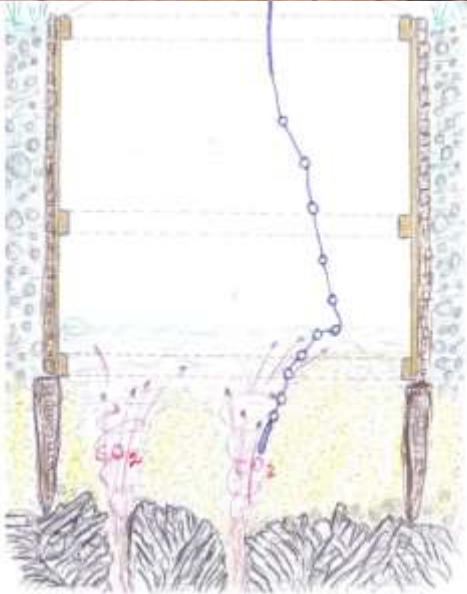
$R = 8.314 \text{ J}/(\text{mol K})$  is the ideal gas constant,

$T, [\text{K}]$  is the absolute temperature and

$T_0 = 298.15 \text{ K}$  is a reference temperature.

$H_0^{cp}$  and  $\alpha$  are constants that can be determined experimentally.

There is a similar relationship between carbon dioxide dissolved in molecular form in water and the concentration of carbon dioxide in gas phase.





# Pokolsár, wet mofette of Covasna, Romania



## Model

Volumetric flux density (Darcy velocity) of water entering the pool at the bottom is:

$$q = v\phi, [m^3/m^2s].$$

Flux density of dissolved carbon dioxide transported by water is:

$$Q = q * [CO_2]_w, [mol/m^2s].$$

Flux density of carbon dioxide gas that separates from water in the form of gas bubbles is

$$Q_b = q([CO_2]_w - [CO_2]_t), [mol/m^2s],$$

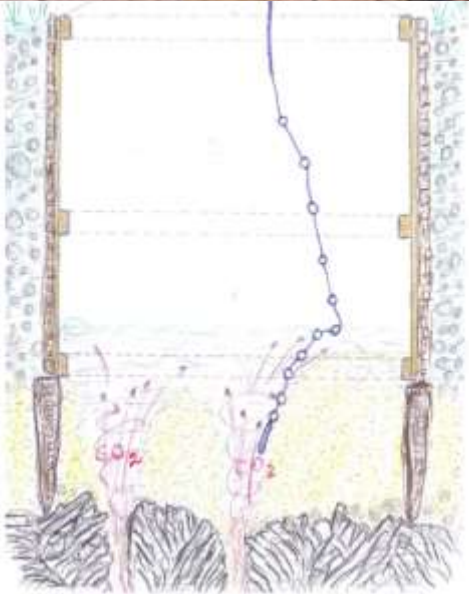
where  $[CO_2]_t = H_{CO_2}^{cp}(T)p_{CO_2}$  is the equilibrium concentration of carbon dioxide dissolved in water at partial pressure of carbon dioxide in bubbles of  $p_{CO_2} = 10^5 Pa$  and at temperature  $T$ . Finally we need to convert the material flux density into a volume flux density. This requires the use of molar concentration of carbon dioxide in the bubbles. According to the ideal gas equation:  $p_{CO_2} = [CO_2]_b RT$ , from which  $[CO_2]_b = p_{CO_2} / (RT)$ .

The volume flux density of carbon dioxide leaving through bubbles is:

$$Q_{bV} = \frac{Q_b}{[CO_2]_b}, [m^3/m^2s].$$

The radon flux density leaving through bubbles is:

$$j_b = Q_{bV}C_b = Q_{bV} \frac{C_w}{H_{Rn}^{cc}(T)}$$



# Pokolsár, wet mofette of Covasna, Romania

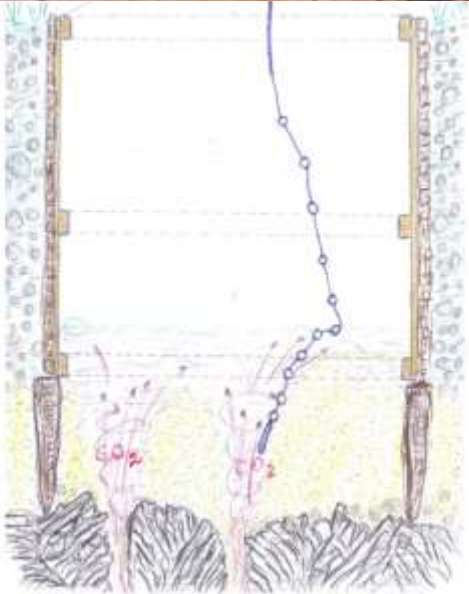


## Model

Substituting all of these in the equation of radon balance of pool space in stationary case:

$$(v - D\gamma_2)e^{\gamma_2 z_2} \phi C_{s0} + v\phi \frac{G_s}{\lambda} - Q_{bv} \frac{C_w}{H_{Rn}^{cc}(T)} - v\phi C_w - \lambda(z_1 - z_2)C_w = 0.$$

from which:



# Pokolsár, wet mofette of Covasna, Romania



## Model

The remaining radon content of the water:

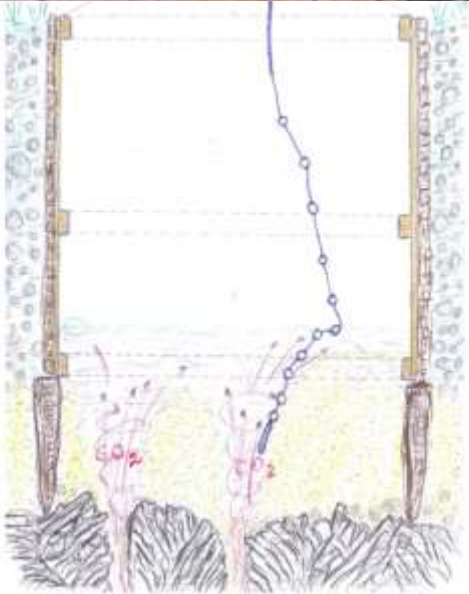
$$C_w = \frac{\frac{\phi \left\{ \frac{(v - D\gamma_2)\gamma_1}{\gamma_2 - \gamma_1} (G_s - G_d)e^{\gamma_2 h_s} + vG_s \right\}}{\frac{Q_{bV}}{H_{Rn}^{cc}(T)} + v\phi + \lambda h_w}}$$

where

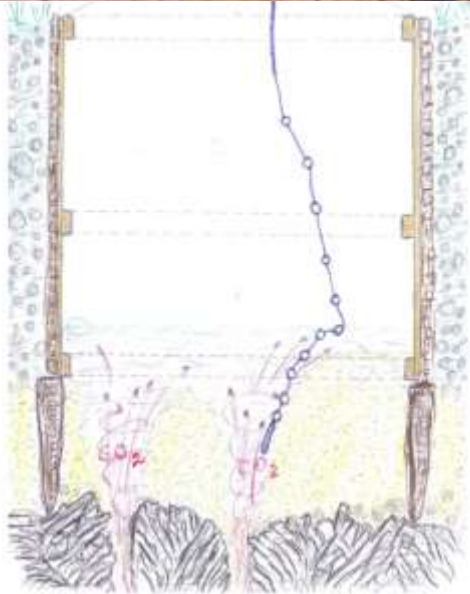
$h_s = (z_2 - z_3)$  is the thickness of the sediment under the bottom of the pool and

$h_w = (z_1 - z_2)$  is the thickness of the water layer in the pool.

**In the water of the wet mofette, carbon dioxide is degassing, and flashes out much of the radon, too.**



# Pokolsár, wet mofette of Covasna, Romania



## Model

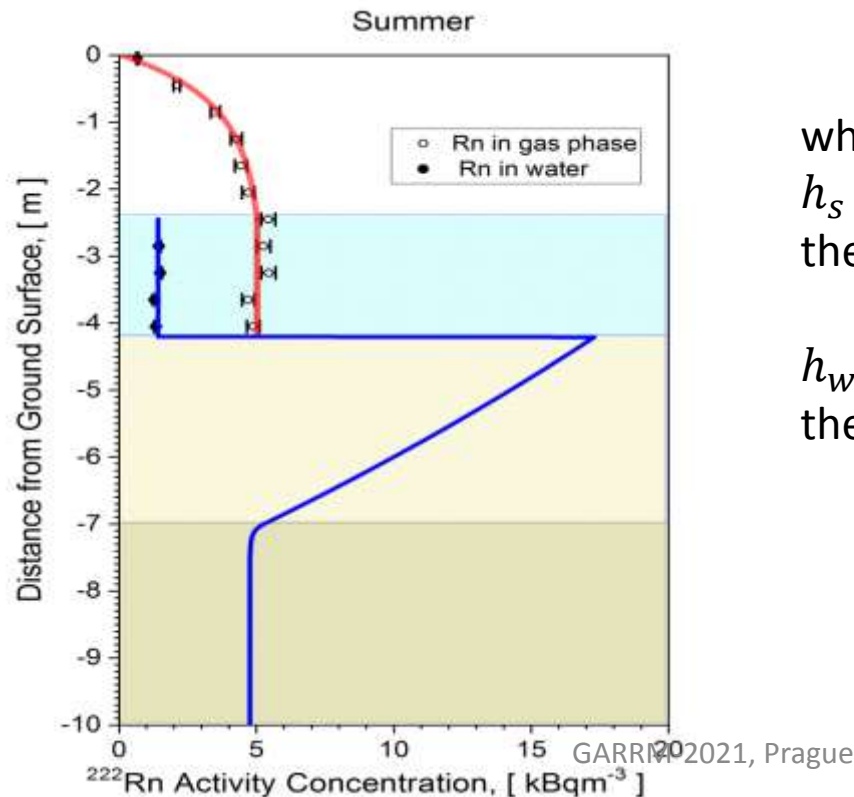
The remaining radon content of the water:

$$C_w = \frac{\frac{\phi}{\lambda} \left\{ \frac{(v - D\gamma_2)\gamma_1}{\gamma_2 - \gamma_1} (G_s - G_d)e^{\gamma_2 h_s} + vG_s \right\}}{\frac{Q_{bV}}{H_{Rn}^{cc}(T)} + v\phi + \lambda h_w}$$

where

$h_s = (z_2 - z_3)$  is the thickness of the sediment under the bottom of the pool and

$h_w = (z_1 - z_2)$  is the thickness of the water layer in the pool.



# Dry mofettes of Covasna, Romania

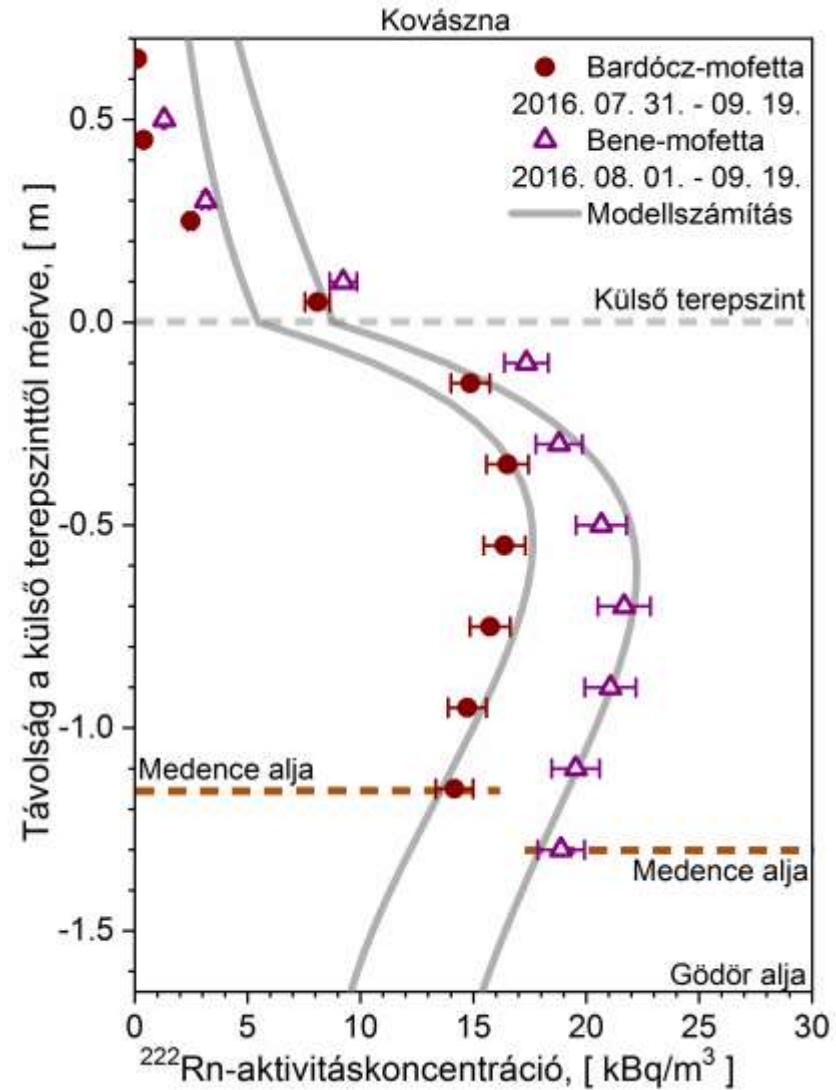
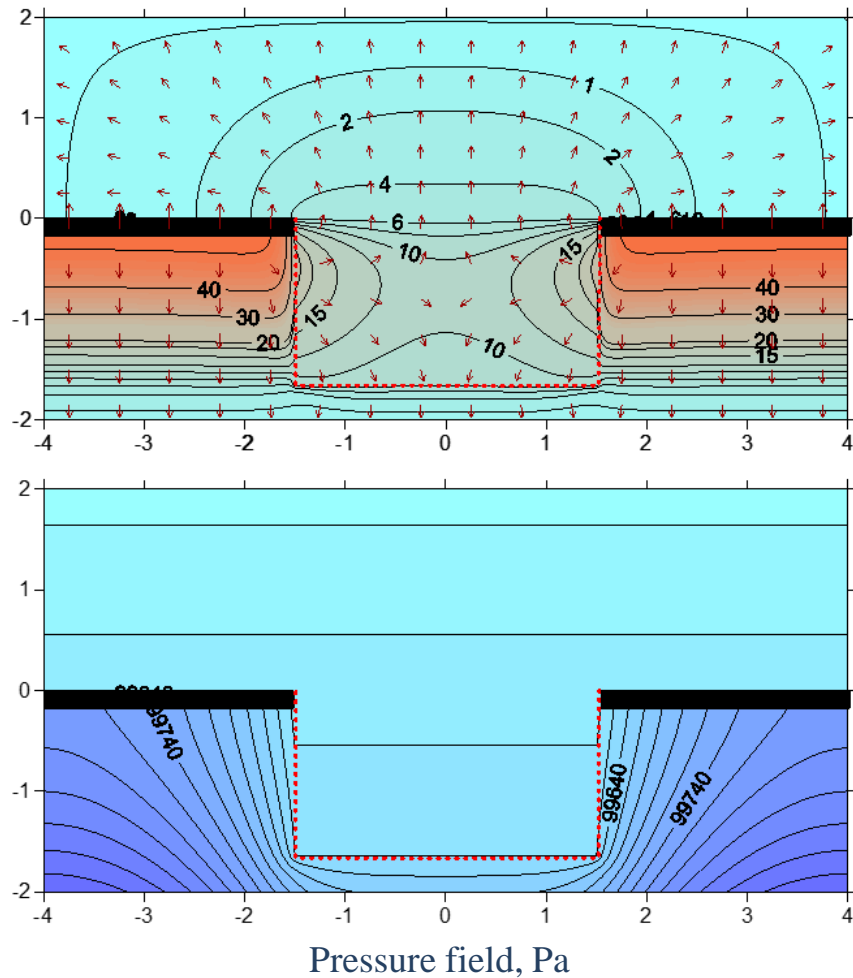


The very same hydrogeological and radon transport model can be applied to both wet and dry mofettes of Covasna!

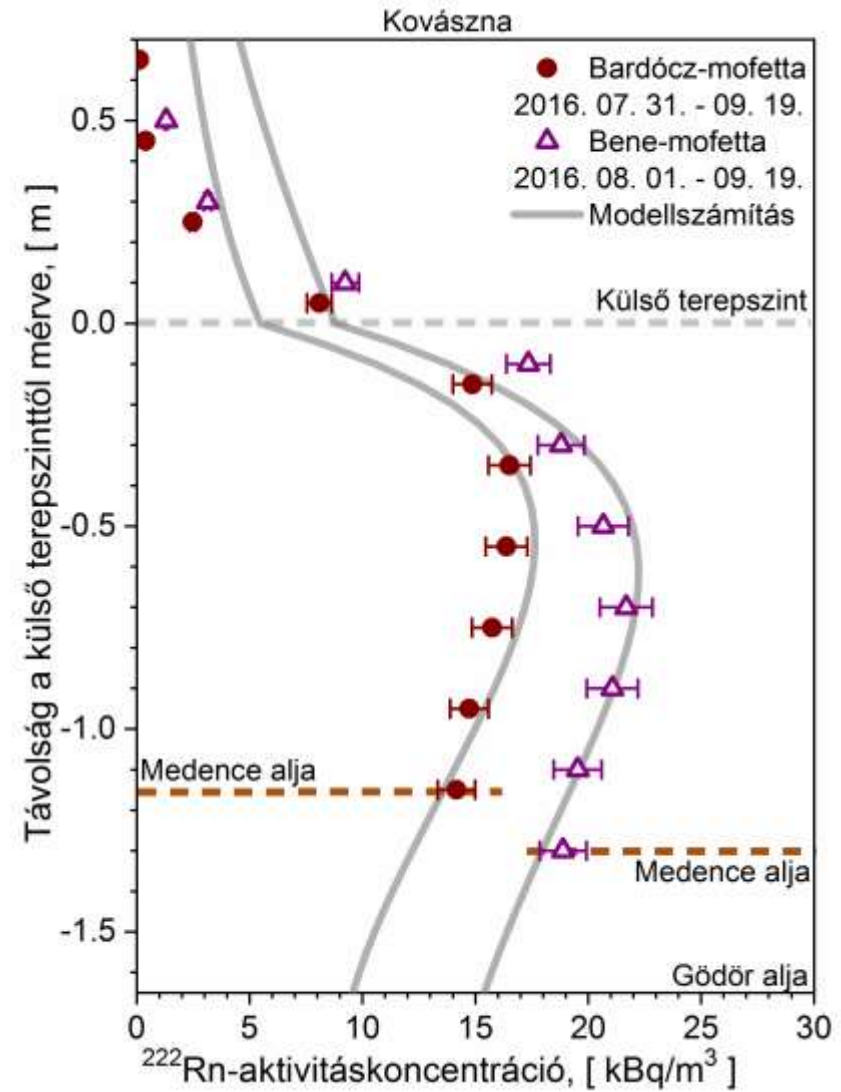
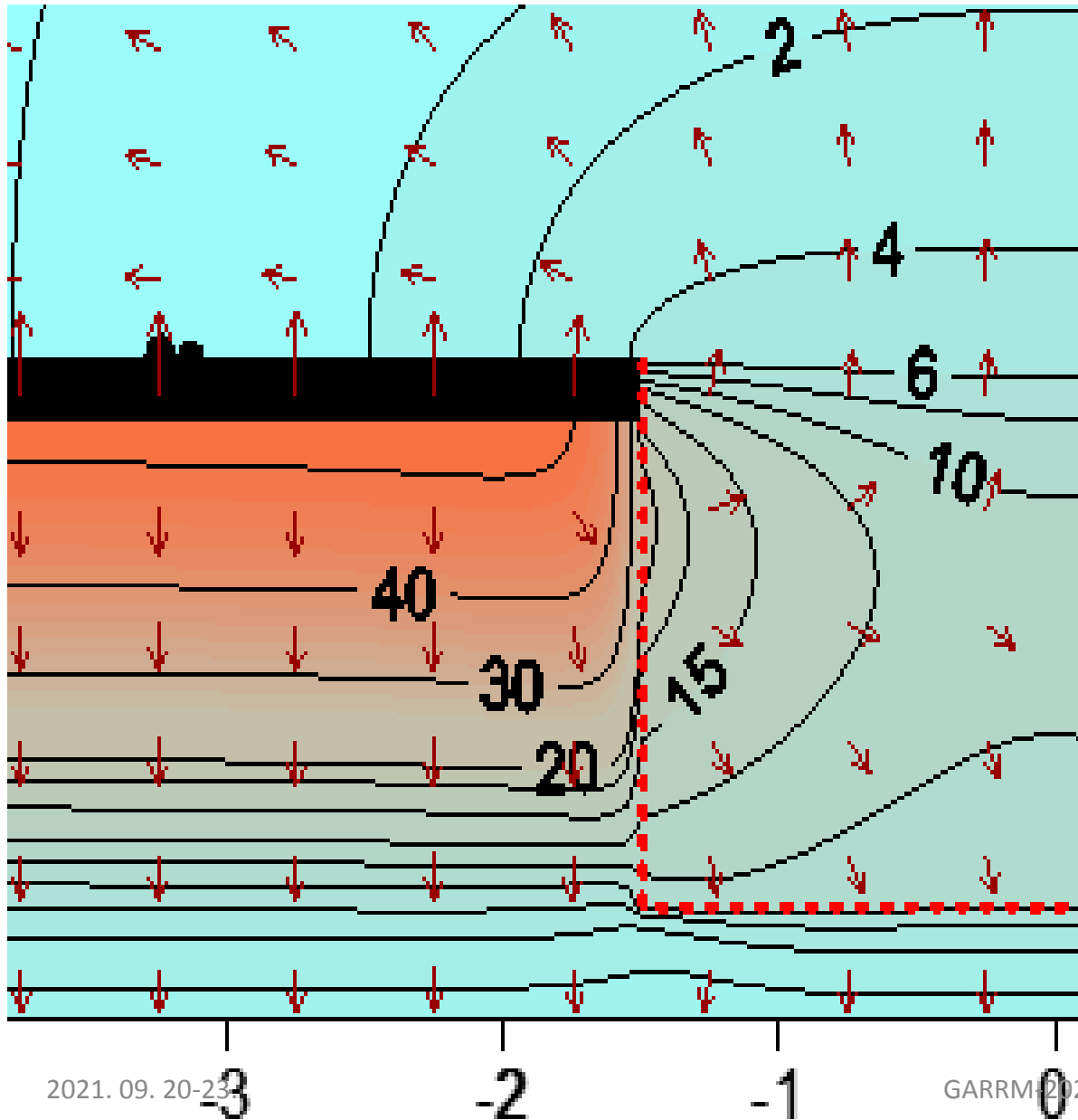


# Dry mofettes of Covasna, Romania

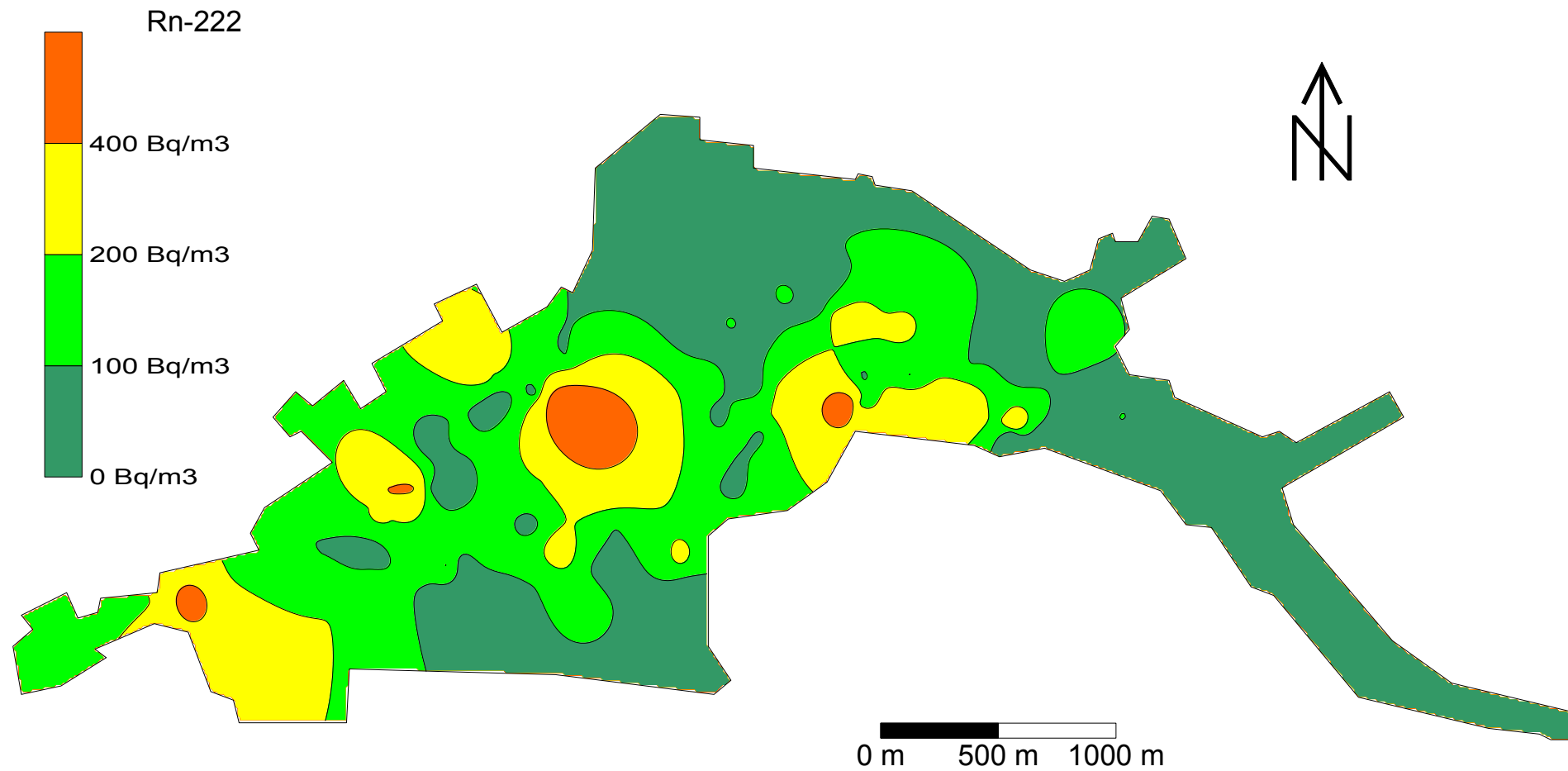
$^{222}\text{Rn}$  activity concentration in soil gas and gas phase of the mofette,  $\text{kBq/m}^3$



# Dry mofettes of Covasna, Romania



# Mapping of Indoor Radon in Kovászna



István Csige and Sándor Csegzi



## **Acknowledgements**

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